

# WU #8 - Interaction & Indicators

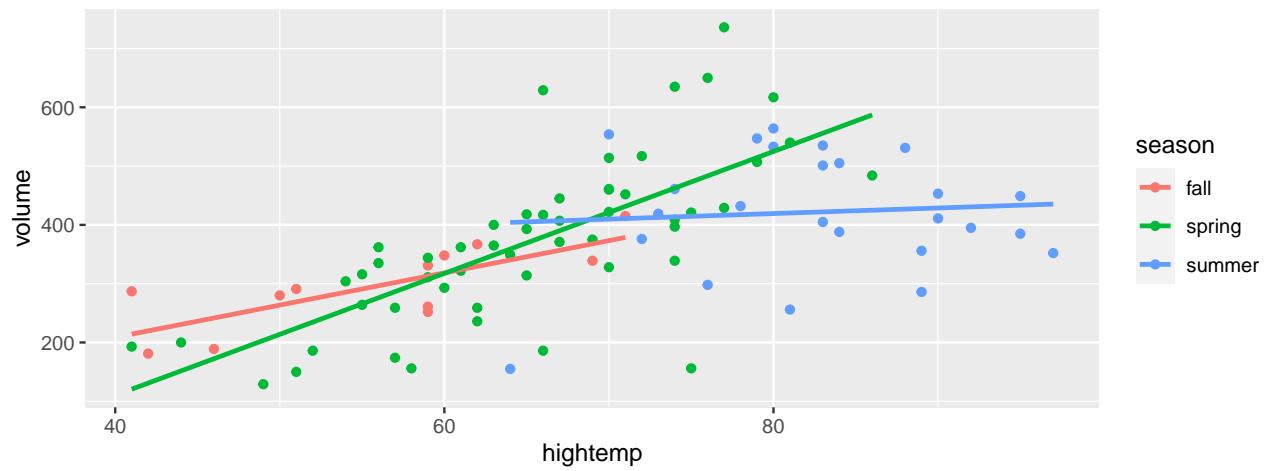
Math 158 - Jo Hardin

Tuesday 2/15/2022

Name: \_\_\_\_\_

Names of people you worked with: \_\_\_\_\_

Consider the `RailTrail` data. The model below regresses `volume` of bicycle riders on `hightemp` and `season`.



```
RailTrail %>%
  lm(volume ~ hightemp * season, data = .) %>%
  tidy()
```

```
## # A tibble: 6 x 5
##   term            estimate std.error statistic p.value
##   <chr>          <dbl>     <dbl>      <dbl>    <dbl>
## 1 (Intercept)    -10.5      167.     -0.0631  0.950
## 2 hightemp        5.48       2.95      1.86    0.0667
## 3 seasonspring   -294.      190.     -1.54    0.126
## 4 seasonsummer    354.      255.      1.39    0.169
## 5 hightemp:seasonspring  4.88      3.26      1.50    0.138
## 6 hightemp:seasonsummer -4.54      3.75     -1.21    0.230
```

Write down three separate models (each of spring, summer, and fall) for how `hightemp` predicts `volume` separately depending on the season. The three answers will each look something like:

$$\text{winter: } \widehat{\text{volume}} = 47 + 0.47 \cdot \text{hightemp}.$$

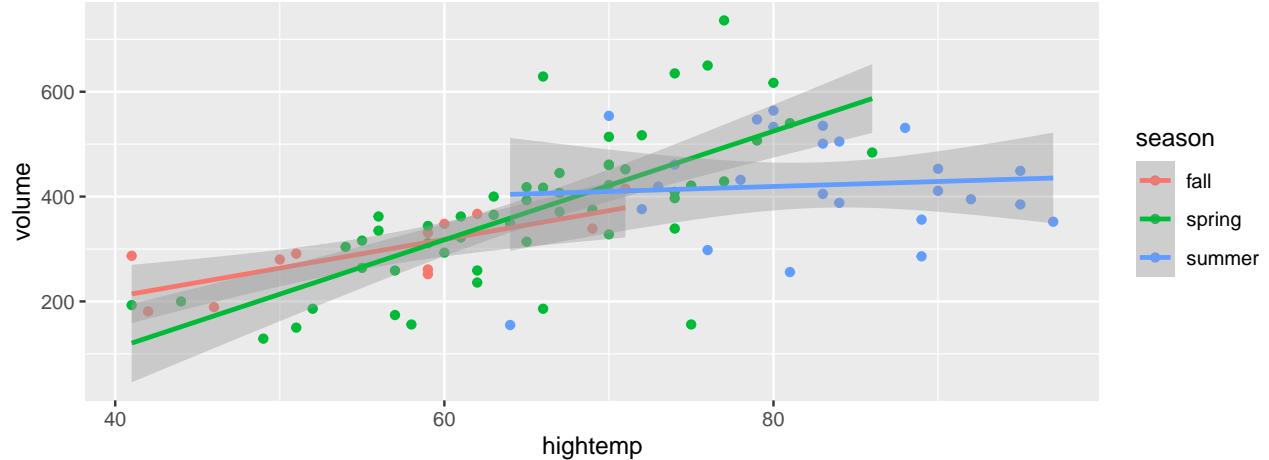
**Solution:**

fall:  $\widehat{\text{volume}} = -10.53 + 5.48 \cdot \text{hightemp}$ .

spring:  $\widehat{\text{volume}} = (-10.53 - 293.95) + (5.48 + 4.88) \cdot \text{hightemp} = -304.48 + 10.36 \cdot \text{hightemp}$ .

summer:  $\widehat{\text{volume}} = (-10.53 + 354.18) + (5.48 + -4.54) \cdot \text{hightemp} = 343.65 + 0.94 \cdot \text{hightemp}$ .

Note that the interaction term is not significant! The lack of significance can be seen if SE ribbons are added to the linear model.



Additionally, if the interaction is removed, the model shows that `hightemp` is significant, but `season` is not.

```
RailTrail %>%
  lm(volume ~ hightemp + season, data = .) %>%
  tidy()
```

```
## # A tibble: 4 x 5
##   term      estimate std.error statistic    p.value
##   <chr>      <dbl>     <dbl>     <dbl>      <dbl>
## 1 (Intercept) -125.      71.7     -1.75  0.0841
## 2 hightemp      7.54      1.17      6.43  0.00000000692
## 3 seasonspring  5.13     34.3      0.150  0.881
## 4 seasonsummer -76.8     47.7     -1.61  0.111
```

```
RailTrail %>%
  lm(volume ~ hightemp, data = .) %>%
  tidy()
```

```
## # A tibble: 2 x 5
##   term      estimate std.error statistic    p.value
##   <chr>      <dbl>     <dbl>     <dbl>      <dbl>
## 1 (Intercept) -17.1      59.4     -0.288  0.774
## 2 hightemp      5.70      0.848      6.72  0.00000000171
```